Biological Applications of Deep Learning Lecture 4

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CONTENTS TODAY

► Reminder: Regularization

Convolutional Neural Networks



Reminder: Dropout, Regularization



L1 VERSUS L2 REGULARIZATION

- ► In L1 regularization, weights shrink by a *constant* amount.
- ► In L2 regularization, weights shrink by an amount *proportionally* to *w*.
- L1 regularization tends to bring forward a small number of high-importance connections.
- L2 regularization tends to keep all weights small.



DROPOUT



Full network, before dropout



DROPOUT



Network after having dropped half of the hidden nodes



DROPOUT

Procedure

- 1. Choose a mini batch of training data of size \hat{m}
- 2. Randomly delete half of the hidden nodes, while keeping all input and output nodes
- 3. Train the resulting network using the mini batch; update all weights and biases
- 4. If validation accuracy not yet satisfying, return to 1.
- 5. After each epoch, decrease each weight by a factor of $\frac{1}{2}$



DROPOUT

EXPLANATIONS

- Dropout can be perceived as averaging over several smaller networks, where averaging over several models is generally helpful to prevent overfitting
- Dropout can be perceived as projecting points in parameter space onto the linear subspace defined by only half of the elementary basis vectors.
- Combining optima in subspaces yields a selection of parameters that are not optimal, but nearby an optimum
 experience shows that this prevents overfitting
- Dropout prevents "co-adaptation of neurons"



L1/2 REGULARIZATION, DROPOUT, EARLY STOPPING TAKE-HOME MESSAGE

Try to find a reasonable point near the very optimum

- L1/2 regularization: shrink or eliminate weights that don't change much
- *Dropout*: Randomly project points to linear subspaces, and optimize there, and then average out
- *Early stopping*: Stop before reaching the optimum



ARTIFICIAL EXPANSION OF TRAINING DATA



More training data improves test accuracy



ARTIFICIAL EXPANSION OF TRAINING DATA



NN versus SVM on same training data

- Sometimes better training data delivers substantial improvements
- Always good to aim for methodical improvements, but:

Don't miss "easy wins" by generating more and/or better training data UNIVERSITÄT BELEFELD

GENERATING ARTIFICIAL TRAINING DATA



Rotating 5 by 15 degrees to the left yields new training datum

Other Techniques

- ► Translating, skewing
- "Elastic distortions"
- For more details, see [Simard, Steinkraus & Platt, 2003] https://ieeexplore.ieee.org/document/1227801

Convolutional Neural Networks (CNNs)



Motivation



GOAL

Setting up a neural network that correctly classifies 9967 out of 10000 images; see below for the 33 misclassified ones.

33 misclassified images; correct/predicted classification upper/lower right corner



FULLY CONNECTED NETWORKS



Fully connected neural network with 3 hidden layers

Issue: With fully connected NN's, we only reach about 98% accuracy in prediction.

Question: How to get to 99,67% accuracy?



Motivation

- ► Use that images have a spatial structure
 - Neighboring pixels are more likely to belong to the same structural elements
- Exploit this to speed up training, and reduce number of parameters (weights)

Basic Ideas

- ► Local receptive fields
- ► Shared weights
- Pooling



Local Receptive Fields and Convolutional Filters



LOCAL RECEPTIVE FIELDS



One image are $28 \times 28 = 784$ pixels

In a fully connected network

- Every node of the first hidden layer is connected to every input neuron (a.k.a pixel)
- Every node of the second layer is connected to every neuron in the first hidden layer



LOCAL RECEPTIVE FIELDS

In a convolutional NN,

- Every node in the first hidden layer is connected to a rectangular subregion
- Here: subregion = square of 5x5=25 input neurons



Convolutional filter of size 5 x 5

Definition

The region in the input images to which a hidden neuron is connected is called the *local receptive field (LRF)* of the hidden neuron.

LOCAL RECEPTIVE FIELDS

input neurons

00000000000000000000000000000000000000

first hidden layer

000000000000000000000000000000000000000	

input neurons

00000	-
000000000000000000000000000000000000000	
000000000000000000000000000000000000000	

first hidden layer



COMPUTING HIDDEN LAYERS

- One *hidden layer* is generated by one pass of the LRF
- Several hidden layers will be generated by several passes of the LRF
- The activation a^{l+1}_{jk} of the j, k-th hidden neuron within the layer, using a M × M LRF, is computed as (σ may represent activation function of choice)

$$a_{jk}^{(l+1)} = \sigma(b + \sum_{l=0}^{M} \sum_{m=0}^{M} w_{l,m} a_{j+l,k+m}^{l})$$
(1)



CONVOLUTIONAL FILTERS



For generating one hidden layer, identical parameters, together defining one convolutional filter, are used



CONVOLUTIONAL FILTERS



For generating one hidden layer, identical parameters, together defining one convolutional filter, are used



CONVOLUTIONAL FILTERS

Definition A *feature map* is a mapping associated with one convolutional filter.



- A complete convolutional layer consists of several hidden sublayers
- Each sublayer is defined by one feature map
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CONVOLUTIONAL FILTERS REAL WORLD EXAMPLE



MNIST example, 20 different filters

- The darker the more positive, the whiter the more negative
- ► In reality, convolutional filters are hard to interpret
- Literature: M.D. Zeiler, R. Fergus, "Visualizing and Understanding Convolutional Networks", https://arxiv.org/abs/1311.2901



Sharing Weights



SHARED WEIGHTS AND BIASES

► *Reminder*: The activation a_{jk}^{l+1} of the *j*, *k*-th hidden neuron within the layer, using a $M \times M$ LRF, is computed as (σ may represent activation function of choice)

$$a_{jk}^{l+1} = \sigma(b + \sum_{l=0}^{M} \sum_{m=0}^{M} w_{l,m} a_{j+l,k+m}^{l})$$
(2)

- ► *Observation:* For each node in the same hidden layer, the same parameters $w_{l,m}$, $1 \le l, m \le M$ are used
- ► That is, we only need *M* × *M* parameters to generate the entire hidden layer



SHARED WEIGHTS AND BIASES

MNIST example

- Convolutional layer, 20 feature maps, each of size 5 × 5, roughly requires 20 × 5 × 5 = 500 weights
- ► Fully connected network, connecting 784 input neurons with 30 hidden neurons requires 784 × 30 = 23 520 weights
- CNN requires roughly 40 times less parameters



:

CONVOLUTIONAL LAYER

- *Remark*: Sometimes it helps to think of a convolutional layer, as a new type of image, where each sublayer refers to a different color.
- ► Note that colored pictures of size N × N come in 3 input layers of size N × N, each of which refers to one of the 3 base colors red, green and blue.
- ► So, when using *M* × *M*-filters, one applies a 3 × *M* × *M* sized *tensor* (and not an *M* × *M*-sized matrix) to the input layer
- This principle can later be repeated: hence the name *tensor flow*.



Pooling Layers



POOLING LAYERS

- In addition to convolutional layers, CNN's make use of pooling layers.
- Pooling layers generate *condensed feature maps*: it takes a rectangle of neurons, and summarizes their values into one value
- This generates a considerably smaller layer



POOLING LAYERS

hidden neurons (output from feature map)



 2×2 pooling

- Max pooling: Each L × L rectangle is mapped onto the maximum of its values
- ► *L2 pooling*: Each *L* × *L* rectangle is mapped to the rooted average of the squares of the values
- This overall yields a layer that is $L \times L$ times smaller
- UNIVERSITÄUsually L = 2 is used

CONVOLUTIONAL NEURAL NETWORKS Combining Convolutional and Pooling Layers



Convolutional layer followed by pooling layer

- Convolutional and pooling layers are used in combination
- Pooling layers usually follow convolutional layers
- ► Intuition:
 - ► The exact location of the occurrence of a feature is not important
 - Pooling helps to handle distortions and rotations



CONVOLUTIONAL NEURAL NETWORKS A COMPLETE CNN



Convolution followed by pooling followed by fully connected output layer

- ► 10 output nodes, one for each digit
- Each output node is connected to *every* node of the pooling layer
- Training: Stochastic gradient descent plus backpropagation



Convolutional Neural Networks in Practice


BASELINE: SIMPLE FULLY CONNECTED NETWORK

► Baseline:

One hidden layer, 100 neurons

- Output layer, cost function: softmax + log-likelihood
- ► Training:
 - ► 60 epochs
 - Learning rate $\eta = 0.1$
 - Mini-batch size 10
- ► Test accuracy: 97.80%



FIRST CNN: ONE COVOLUTION-POOLING LAYER



Inserting a convolution and max-pooling layer

- ► Convolutional layer:
 - 5×5 LRFs, stride length 1
 - 20 feature maps
- ► Pooling layer:
 - ► 2 × 2 max-pooling

univeRitäAccuracy: 98.78% test accuracy

TWO CONVOLUTION-POOLING LAYERS

- ► 2 Convolutional layers:
 - ► *First convolution*: 20 feature maps, each associated with 5 × 5 LRFs, stride length 1
 - Second convolution: 40 feature maps, each associated with $20 \times 5 \times 5$ filter, stride length 1
- ► Pooling layer:
 - ► 2 × 2 max-pooling



- So, each LRF is a $20 \times 12 \times 12$ tensor
- Spatial strucure is still preserved in second conv-pooling layer, so employing conv-pooling makes sense

UNIVERSITE Accuracy: 99.06% test accuracy

TRYING ALTERNATIVE ACTIVATION FUNCTIONS

- ► Tanh activation function:
 - Training is (a bit) faster
 - Results are near-identical
 - ► Explanation:

$$\sigma(z) = \frac{1 + \tanh(z/2)}{2} \tag{3}$$



Activation:

$$f(z) = \max(0,z)$$

- Learning rate: $\eta = 0.03$ (earlier: 0.1)
- L2 regularization at $\lambda = 0.1$
- ► Test accuracy: 99.23%
- Modest gain, but also in other experiments ReLUs have shown to consistently outperform sigmoid neurons



EXPANDING THE TRAINING DATA

- ► *Experiment*:
 - Displace each image by one pixel to above, the right, below, or to the left
 - ► Each image has 4 extra copies
 - 250 000 images instead of 50 000
- ▶ Run the same network with ReLU's (99.23%)
- ► Expanding training data yields 99.37%
- P. Simard, D. Steinkraus, J. Platt, "Best Practices for Convolutional Neural Networks Applied to Visual Document Analysis", 2003:
 - ► Very similar architecture
 - Training data expansion: rotations, translations, skewing
 - "Elastic distortions": emulating random oscillations of hand muscles
 - ► Accuracy: 99.6%



EXTRA/LARGER FULLY CONNECTED LAYER

► Larger fully connected layer:

- ► 300 neurons 🖙 accuracy: 99.46%
- ▶ 1000 neurons IS accuracy: 99.43%
- Not really convincing
- ► Extra fully connected layer:
 - ► 2 fully connected layers, each of 100 neurons S accuracy 99.43%
 - ► 2 fully connected layers, each of 300/1000 neurons accuracy 99.47/99.48%
- No convincing improvements



DROPOUT

- ► 2 fully connected layers each of 1000 neurons
- Dropout (probability = 0.5) applied to neurons in fully connected layers
- Accuracy: 99.6% (which is substantial improvement)
- ► Remarks:
 - ► Less epochs (40 instead of 60), because of faster training
 - More hidden neurons (1000 instead of 300 or 100) slightly preferable when using dropout
 - No dropout on convolutional layers: those have in-built resistance to overfitting because of parameter sharing



ENSEMBLE OF NETWORKS

Ensemble of networks: Idea

- Train several different networks
- For example, employ repeated random initialization while always using the same architecture
- For classification, take the majority vote of the different networks
- While each network performs similarly, the majority vote may yield improvements
- Here: 5 randomly initialized network of the architecture o described in the slides before
- ► Accuracy: 99.67%
- ► That has been our goal!



ENSEMBLE OF NETWORKS

- Ensemble of 5 randomly initialized networks
- Architecture as described in the slides before
- ► Accuracy: 99.67% that has been our goal!



23 misclassified images; correct/predicted classification upper/lower right corner BIELEFELD

References

Y. LeCun, L. Bottou, Y. Bengio, P. Haffner, "Gradient-based learning applied to document recognition", http:// yann.lecun.com/exdb/publis/pdf/lecun-98.pdf [Architecture: "LeNet-5"]



CNNs on MNIST

FURTHER IMPROVEMENTS

For further improvements on MNIST (and on famous datasets in general see http://rodrigob.github.io/are_we_there_yet/ build/classification_datasets_results.html

- ► Noteworthy:
 - See D.C. Ciresan, U. Meier, L.M. Gambardella, J. Schmidhuber, "Deep Big Simple Neural Nets Excel on Handwritten Digit Recognition", https://arxiv.org/abs/1003.0358
 - Fully connected network, without convolutional layers that achieves 99.65% accuracy.
 - Training for that non-convolutional network proceeds very slow, however.



LECTURE4: SUMMARY

Convolutional Neural Networks

- http://www.deeplearningbook.org/, Chapter 9
- http://neuralnetworksanddeeplearning.com/, "Deep Learning"



Outlook

Choosing hyperparameters

- http://www.deeplearningbook.org/, Chapter 11 (selected parts)
- http://neuralnetworksanddeeplearning.com/, "Weight initialization" and "How to choose a network's hyperparameters?"
- Convolutional backpropagation
 - ► For further illustrations, see

https://medium.com/@2017csm1006/

forward-and-backpropagation-in-convolutional-neural-network-

Note that there notation differs (error *E* there is cost *C* here, *X* there is *z* here, and *F* are the weights *w* here, and *O* is *a* here, and there is no bias)

Training variations

- http://www.deeplearningbook.org/, Chapter 8 (corresponding parts)
- http://neuralnetworksanddeeplearning.com/, Chapter
 - 3, "Variations on stochastic gradient descent"

Thanks for your attention

